

ex. 3 $(P + 5V^{-2})(V - .03) = 9.7$ $\begin{pmatrix} 5 \\ 1 \end{pmatrix}$
 $\begin{pmatrix} P \\ V \end{pmatrix}$

$$\frac{dV}{dP} = V'(P) \quad (1 - 10V^{-3}V'(P))(V - .03) + (P + 5V^{-2})V'(P) = 0$$

$$\underbrace{V - .03}_{-V + .03} - 10V^{-2}V'(P) + 3V^{-3}V'(P) + PV'(P) + 5V^{-2}V'(P) = 0$$

$$V'(P) \left(-10V^{-2} + 3V^{-3} + P + 5V^{-2} \right) = .03 - V$$

$$V'(P) \left(-5V^{-2} + 3V^{-3} + P \right) = .03 - V$$

$$V'(P) = \frac{.03 - V}{-5V^{-2} + 3V^{-3} + P} \quad \text{at } (5, 1)$$

$$\text{at } (5, 1) = \frac{.03 - 1}{-5(1)^{-2} + 3(1)^{-3} + 5} = \frac{-.97}{.3} = \left(-\frac{97}{30} \right)$$

Book $\frac{dV}{dP} = \frac{.03 - V}{-10V^{-3}(V - .03) + P + 5V^{-2}}$

ex. Q ^{2nd derivative} $2xy^3 - 5y^2 + 4x = 7$

$$2y^3 + 2x(3y^2)y'(x) - 10y y'(x) + 4 = 0$$

$$2y^3 + 6xy^2 y'(x) - 10y y'(x) + 4 = 0$$

$$6y^2 y'(x) + 6y^2 y'(x) + 2y y'(x)(6x) y'(x) + y''(x)(6xy^2)$$

$$-10y'(x)y'(x) - 10y y''(x) = 0$$

$$12y^2 y'(x) + 12xy [y'(x)]^2 - 10[y'(x)]^2 = 10y y''(x) - 6xy^2 y''(x)$$

$$12y^2 y'(x) + 12xy [y'(x)]^2 - 10[y'(x)]^2 = y''(x)(10y - 6xy^2)$$

$$\frac{12y^2 y'(x) + 12xy [y'(x)]^2 - 10[y'(x)]^2}{10y - 6xy^2} = y''(x)$$

p. 224-225

1-19 odd, 25