13. $3e^{-2x} - 5 = 4$

$3e^{-2x} = 9$

$e^{-2x} = 3$

$\ln e^{-2x} = \ln 3$

$-2x = \ln 3$

$x = \dfrac{\ln 3}{-2}$

$x \approx -.5493$

$-2x \ln e$

$-2x(1)$

$\ln(3)/-2$

18. $\ln(3x + 4) = -7$

$e^{\ln(3x+4)} = e^{-7}$

$3x + 4 = e^{-7}$

$3x = e^{-7} - 4$

$x = \dfrac{(e^{-7} - 4)}{3}$

$x \approx -1.3330$

$(e^{\wedge}(-7) - 4)/3$

23. Suppose you deposit $1000 in an account paying 2% annual interest, compounded continuously, how many years would It take for your account to be worth $2000?

$$A = Pe^{rt}$$

$$2000 = 1000e^{.02t} \qquad t = 34.6574 \text{ yrs}$$

$$2 = e^{.02t} \qquad\qquad 34.7$$

$$\ln 2 = \ln e^{.02t} \qquad\quad 35$$

$$\ln 2 = .02t$$

$$\frac{\ln 2}{.02} = t$$

Section 9.6 - Exponential Growth and Decay

Exponential Growth: $y = a(1 + r)^t$ $\qquad$ $y = a(b)^x \quad b > 1$

Exponential Decay: $y = a(1 - r)^t$ $\qquad$ $y = a(b)^x \quad 0 < b < 1$

Where y is the amount of a quantity that exists/remains after t time periods given an initial amount a and r is the percent of increase/decrease expressed as a decimal.

2. In 1910, the population of a city was 120,000. Since then, the population has increased by 1.5% per year. If the population continues to grow at this rate, what will the population be in 2010?

$$y = a(1 + r)^t$$
$$y = 120,000(1 + .015)^{100}$$
$$y = 120,000(1.015)^{100}$$
$$y = 531,845 \quad \text{people}$$

1. A cup of coffee contains 130 milligrams of caffeine. If caffeine is eliminated from the body at a rate of 11% per hour, how long will it take for half of this caffeine to be eliminated?

$$y = a(1-r)^t$$

$$\log_b m^p = p \log_b m$$

$$\frac{65}{130} = \frac{130(1-.11)^t}{130}$$

$$.5 = .89^t$$

$$\log .5 = \log .89^t \qquad OR \qquad \ln .5 = \ln .89^t$$

$$\frac{\log .5}{\log .89} = \frac{t \log .89}{\log .89} \qquad\qquad \frac{\ln .5}{\ln .89} = \frac{t \ln .89}{\ln .89}$$

$$t \approx 5.948 \text{ hrs}$$

5.95
5.9
6