

6. ~~$\log_7 x$~~ $= \log_7 27 + \log_7 3$

$$\log_7 x^2 = \log_7 81$$

$$\sqrt{x^2} = \sqrt{81}$$

$$x = \pm 9$$

$$x = 9$$

$$\cdot \log_7 (-9)$$

$$7^a = -9$$

7. $\log_6(x-2) + \log_6(x+3) = \log_6 14$

$$\log_6(x^2 + x - 6) = \log_6 14$$

$$x^2 + x - 6 = 14$$

quadratic form, $x^2 + x - 20 = 0$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$x = \frac{-1 \pm \sqrt{1^2 - 4(1)(-20)}}{2(1)}$$

factoring

$$(x-4)(x+5) = 0$$

$x-4=0$	$x+5=0$
$x=4$	$x=-5$

$$x = -\frac{1 \pm \sqrt{81}}{2} = \frac{-1 \pm 9}{2} = \frac{-1+9}{2} \text{ or } \frac{-1-9}{2}$$

$$x = 4 \quad \text{or} \quad \cancel{-5}$$

$$8. \log_6 x - \log_6(x-5) = \log_6 2$$

$$\log_6\left(\frac{x}{x-5}\right) = \log_6 2$$

$$\cancel{(x-5)} \frac{x}{x-5} = 2^{\cancel{(x-5)}}$$

$$x = 2x - 10$$

$$\begin{aligned} -x &= -10 \\ x &= 10 \end{aligned}$$

$$9. \log_2 4x - \log_2 5 = 6$$

$$\log_2 \frac{4x}{5} = 6$$

$$(5) 2^6 = \frac{4x}{5} (5)$$

$$320 = 4x$$

$$80 = x$$

$$\begin{array}{l} \log_b x = y \\ \downarrow \text{exp. form} \\ b^y = x \end{array}$$

10. $\log_4 x + \log_4(x-6) = 2$

$$\log_4(x^2 - 6x) = 2$$

$$\rightarrow 4^2 = x^2 - 6x$$

$$0 = x^2 - 6x - 16$$

$$X = \frac{b \pm \sqrt{(-6)^2 - 4(1)(-16)}}{2(1)}$$

$$X = \frac{6 \pm \sqrt{100}}{2}$$

$$X = \frac{6 \pm 10}{2} = \frac{6+10}{2} \text{ or } \frac{6-10}{2}$$

$$X = 8, \quad \cancel{X = -2}$$

$$0 = (x-8)(x+2)$$

$$x-8=0 \quad x+2=0$$

$$X = 8 \quad X = -2$$

X	x^2	-8x
2	$2x$	-16