

1 Given $f(x) = x^2 - 3x + 1$ and $g(x) = 4x + 5$, find each function.

$$\begin{aligned}(f+g)(x) &= f(x) + g(x) = (x^2 - 3x + 1) + (4x + 5) \\ &= x^2 - \underline{3x} + \underline{1} + \underline{4x} + \underline{5}\end{aligned}$$

$$(f+g)(x) = x^2 + x + 6$$

$$\begin{aligned}(f-g)(x) &= f(x) - g(x) = (x^2 - 3x + 1) - (4x + 5) \\ &= x^2 - \underline{3x} + \underline{1} - \underline{4x} - \underline{5}\end{aligned}$$

$$(f-g)(x) = x^2 - 7x - 4$$

$$\begin{aligned}(f \cdot g)(x) &= f(x) \cdot g(x) = (x^2 - 3x + 1)(4x + 5) \\ &= 4x^3 + \underline{5x^2} - \underline{12x^2} - \underline{15x} + \underline{4x} + 5\end{aligned}$$

$$(f \cdot g)(x) = 4x^3 - 7x^2 - 11x + 5$$

$$\left(\frac{f}{g}\right)(x) = \frac{f(x)}{g(x)}, g(x) \neq 0 = \left(\frac{x^2 - 3x + 1}{4x + 5}, x \neq -\frac{5}{4}\right) = \left(\frac{f}{g}\right)(x)$$

$$4x + 5 = 0$$

$$4x = -5$$

$$x = -\frac{5}{4}$$

Composition of functions

$$\underline{[f \circ g](x) = f[g(x)]} = f(g(x))$$

$$f(x) = x + 4$$

$$f(8) = 8 + 4 = 12$$

$$f(y) = y + 4$$

$$f(m+7) = (m+7) + 4 = m + 11$$

$$f(x) = x - 9$$

$$g(x) = 2x + 5$$

$$[f \circ g](x)$$

$$[g \circ f](x) =$$

$$f[g(x)] = f(2x+5) = (2x+5) - 9$$

$$g[f(x)] = g(x-9)$$

$$\underline{[f \circ g](x) = 2x - 4}$$

$$= 2(x-9) + 5$$

$$= 2x - 18 + 5$$

$$\underline{[g \circ f](x) = 2x - 13}$$

$$f(x) = 3x - 1$$

$$g(x) = \underline{x + 4}$$

$$[f \circ g](x) = f(g(x))$$

$$[g \circ f](x) = g(f(x))$$

$$= f(x+4) = 3(x+4) - 1$$

$$= g(3x-1) = (3x-1) + 4$$

$$\underline{[f \circ g](x) = 3x + 11}$$

$$\underline{[g \circ f](x) = 3x + 3}$$

p. 389-390

15-16, 28-31, 33-42,

46-47, 56-57