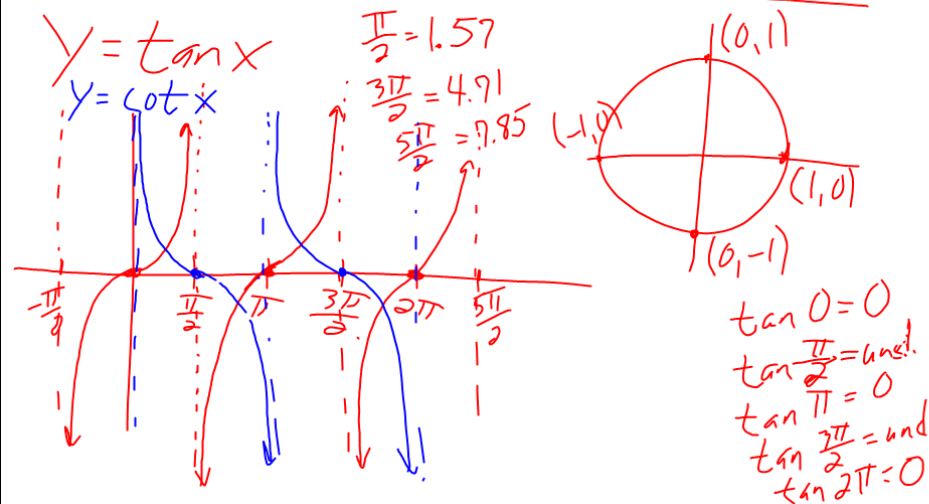


$$\left. \begin{aligned} y &= \csc(kx - c) + h \\ y &= \sec(kx - c) + h \end{aligned} \right\} \begin{aligned} \text{Period} &= \frac{2\pi}{k} \\ \text{P.S.} &= \frac{c}{k} \\ \text{V.S.} &= h \end{aligned}$$



$$y = \csc(k\theta - c) + h$$

$$y = \sec(k\theta - c) + h$$


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$$\text{Period} = \frac{2\pi}{k}$$

$$\text{Phase Shift} = \frac{c}{k}$$

$$\text{Vert. Shift} = h$$

$$y = \tan(k\theta - c) + h$$

$$y = \cot(k\theta - c) + h$$


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$$\text{Period} = \frac{\pi}{k}$$

$$\text{P.S.} = \frac{c}{k}$$

$$\text{V.S.} = h$$

$$y = \csc\left(\frac{\theta}{2} - \frac{\pi}{4}\right) + 2. \quad \text{Find Period, P.S., V.S.}$$

$$k = \frac{1}{2} \quad c = \frac{\pi}{4} \quad h = 2$$

$$\text{Period} = \frac{2\pi}{\frac{1}{2}} = 2\pi \cdot \frac{2}{1} = 4\pi$$

$$\text{P.S.} = \frac{\pi/4}{\frac{1}{2}} = \frac{\pi}{4} \cdot \frac{2}{1} = \frac{\pi}{2}$$

$$\text{V.S.} = 2$$


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$$y = \tan\left(\frac{\theta}{3} + \frac{\pi}{4}\right) - 3$$

$$k = \frac{1}{3} \quad c = -\frac{\pi}{4} \quad h = -3$$

$$\text{Per} = \frac{\pi}{\frac{1}{3}} = 3\pi$$

$$\text{P.S.} = \frac{-\pi/4}{\frac{1}{3}} = -\frac{\pi}{4} \cdot \frac{3}{1} = -\frac{3\pi}{4}$$

$$\text{V.S.} = -3$$

5 Write an equation for a secant function with period  $\pi$ , phase shift  $\frac{\pi}{3}$ , and vertical shift  $-3$ .

$$\begin{aligned} \text{Per} = \pi &= \frac{2\pi}{k} & \text{P.S.} &= \frac{\pi}{3} = \frac{c}{2} \cdot 2 & h &= -3 \\ k &= \frac{2\pi}{\pi} & & & & \\ k &= 2 & \frac{2\pi}{3} &= c & & \end{aligned}$$

$$y = \sec\left(2\theta - \frac{2\pi}{3}\right) - 3$$

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p. 401-403

29-34  $\rightarrow$  no graph  $\rightarrow$  Find Period, Phase Shift, Vert. Shift

36-43, 47, 49, 59