

25. The equation of the axis is $y = 6$, the focus is at $(0, 6)$, and $p = -3$.

$$\text{Focus } (h+p, k) \\ (0, 6)$$

$$h+p = 0 \\ h-3 = 0 \\ h = 3$$

21. $\underline{\underline{2x^2 - 12y - 16x + 20 = 0}}$

$$2(x^2 - 8x + \underline{\underline{16}}) = 12y - 20 + \underline{\underline{2(16)}}$$

$$\frac{2(x-4)^2}{2} = \frac{12y + 12}{2}$$

$$\begin{aligned} (x-4)^2 &= 6y + 6 \\ \frac{(x-4)^2}{2} &= 6(y+1) \\ (x-4)^2 &= 4\left(\frac{3}{2}\right)(y+1) \end{aligned}$$

$6 = 4p$
 $\frac{6}{4} = p$

$$h = 4 \\ k = -1 \\ p = \frac{3}{2}$$

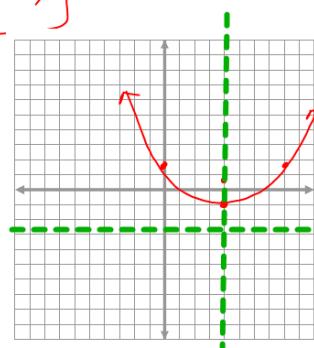
vertex $(4, -1)$
focus $(4, \frac{1}{2})$
directrix: $y = -\frac{5}{2}$
axis of symmetry: $x = 4$

$$(x-4)^2 = 6(y+1)$$

$$16 = 6y + 6$$

$$10 = 6y$$

$$\frac{10}{6} = \frac{5}{3} = y$$



26. The focus is at $(4, -1)$, and the equation of the directrix is $y = -5$.

$$\begin{array}{l} \left| \begin{array}{l} -1 = k + p \\ -1 = -3 + p \\ 2 = p \end{array} \right. \\ \text{directrix} \quad \left| \begin{array}{l} \bullet F(4, -1) \\ \bullet V(4, -3) \\ \cdots \cdots \quad y = -5 \end{array} \right. \end{array}$$

$$(x-h)^2 = 4p(y-k)$$

$$(x-4)^2 = 4(2)(y+3)$$

$$\begin{array}{l} h=4 \\ k=-3 \end{array}$$

(23) $\frac{2y^2 + 16y}{-16x} + \frac{16x + 64}{-64} = 0$

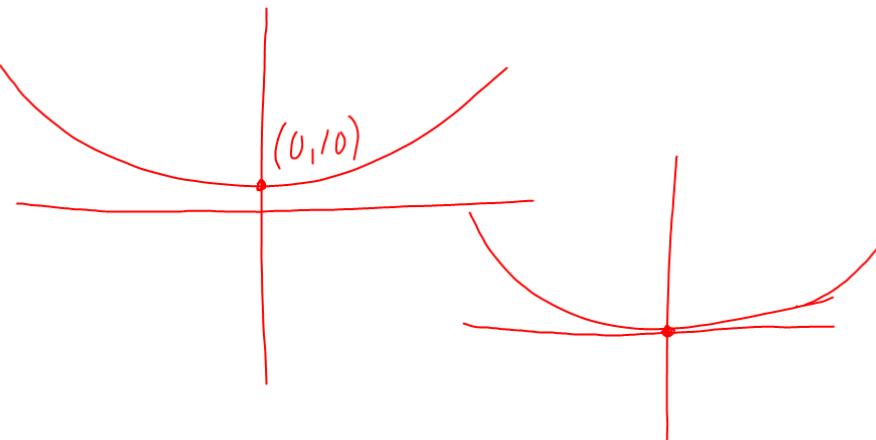
$$2(y^2 + 8y + 16) = -16x - 64 + 2(-16)$$

$$2(y + 4)^2 = -16x - 32$$

$$\frac{2(y + 4)^2}{2} = \frac{-16(x + 2)}{2}$$

$$(y + 4)^2 = -8(x + 2)$$

$$(y + 4)^2 = 4(-2)(x + 2)$$



General form for ALL conic sections

If $A=C$

If A, C same sign

If A, C opposite signs

If A or $C = 0$

| Identify the conic section represented by each equation.

a. $6y^2 + 3x - 4y - 12 = 0$

b. $3y^2 - 2x^2 + 5y - x - 15 = 0$

c. $9x^2 + 27y^2 - 6x - 108y + 82 = 0$

d. $4x^2 + 4y^2 + 5x + 2y - 150 = 0$